



Práctica 1

Desigualdades - Valor absoluto

Resuelva las siguientes desigualdades:

1. $x^2 - x < 6$

$S : (-2, 3)$

2. $3x^2 - x - 2 > 0$

$S : (-\infty, -\frac{2}{3}) \cup (1, \infty)$

3. $\frac{2x-5}{x-2} \leq 1$

$S : (2, 3]$

4. $x^3 - 5x^2 + 4x \leq 0$

$S : (-\infty, 0] \cup [1, 4]$

5. $(x+1)(x-1)^2(x-3) \leq 0$

$S : [-1, 3]$

6. $x^2 - 2x - 4 \leq 0$

$S : [1 - \sqrt{5}, 1 + \sqrt{5}]$

7. $|3x+1| < 2|x-6|$

$S : (-13, \frac{11}{5})$

8. $\left|2 + \frac{5}{x}\right| > 1$ $S : (-\infty, -5) \cup (-\frac{5}{3}, 0) \cup (0, \infty)$

9. $|x-3| < \delta \Rightarrow |6x-18| < \epsilon$

10. $|2x+3| \leq 1$

$S : [-2, -1]$

11. $|2x+4| - |x-1| \leq 4$

$S : [-9, \frac{1}{3}]$

12. $\frac{x}{x+2} < 0$

$S : (-2, 0)$

13. $\frac{2x+1}{1-x} \leq \frac{x+2}{1-x}$

$S : \mathbb{R} \setminus \{1\}$

14. $x^3 - 6x^2 + 11x - 6 > 0$ $S : (1, 2) \cup (3, \infty)$

15. $\left| \frac{x-1}{2-x} \right| \geq 1$ $S : [\frac{3}{2}, 2) \cup (2, \infty)$

16. $\frac{(x^2 - 1)(2x + 4)}{x(3 - x)} > 0$
 $S : (-\infty, -2) \cup (-1, 0) \cup (1, 3)$

17. $\frac{1}{1+x^2} \geq 6.$

18. $|x^2 - 2x - 4| > 4.$

19. $\left| \frac{x-3}{x+5} \right| \leq 1.$

20. $\left| \frac{-2x^2 - 4x - 2}{x^2 + x - 2} \right| \leq 1.$

21. $|x(x-1)| < |x+3|.$

22. $\frac{\sqrt{2x^2 - 8}}{|x-3|} > 1$

23. $\frac{|x^2 + 6x - 7|(x+1)}{x} > 0$

24. $\left| \frac{-2x^2 - 4x - 2}{x^2 + x - 2} \right| \leq 1$

25. $\frac{(x-3)^7(x-2)^6(x^3+1)}{(x-1)^2(2x+1)} \leq 0$

26. $|x^2 - 2x - 3| \geq x + 2$

27. $\frac{|x+3|+x}{x+2} > 1$

28. $x-7 < 2x-5;$ $S : (-2, \infty)$

29. $3x-5 < 4x-6.$

30. $7x-2 \leq 9x+3;$ $S : [-5/2, \infty]$

31. $5x-3 > 6x-4$

32. $10x+1 > 8x+5;$ $S : (2, \infty)$

33. $-2x+5 \geq 4x-3$

34. $-4 < 3x+2 < 5;$ $S : (-2, 1)$

35. $-3 < 4x - 9 < 11$
36. $-3 < 1 - 6x \leq 4;$ S: $[-\frac{1}{2}, \frac{2}{3})$
37. $4 < 5 - 3x < 7$
38. $2 + 3x < 5x + 1 < 16;$ S: $(1/2, 3)$
39. $2x - 4 \leq 6 - 7x \leq 3x + 6$
40. $x^2 + 2x - 12 < 0;$ S: $(-1 - \sqrt{13}, -1 + \sqrt{13})$
41. $x^2 - 5x - 6 > 0$
42. $2x^2 + 5x - 3 > 0;$ S: $(-\infty, -3) \cup (1/2, \infty)$
43. $4x^2 - 5x - 6 < 0$
44. $x^2 - 3x - 4 \geq 0;$ S: $(-\infty, -1] \cup [4, \infty)$
45. $x^2 - 4x + 4 \leq 0;$
46. $3x^2 + 17x - 6 > 0;$ S: $(-\infty, -6) \cup (1/3, \infty)$
47. $14x^2 + 11x - 15 \leq 0;$
48. $\frac{x+4}{x-3} \leq 0;$ S: $[-4, 3)$
49. $\frac{3x-2}{x-1} \geq 0$
50. $\frac{2}{x} < 5;$ S: $(-\infty, 0) \cup (2/5, \infty)$
51. $\frac{7}{4x} \leq 7$
52. $\frac{1}{3x-2} \leq 4;$ S: $(-\infty, 2/3) \cup [3/4, \infty)$
53. $\frac{3}{x+5} > 2;$
54. $(2x-3)(x-1)^2(x-3) \geq 0;$ S: $(-\infty, 3/2] \cup [3, \infty)$
55. $(2x-3)(x-1)^2(x-3) > 0$
56. $(x+2)(x-1)(x-3) > 0;$ S: $(-2, 1) \cup (3, \infty)$
57. $(2x+3)(3x-1)(x-2) < 0$
58. $x^3 - 5x^2 - 6x < 0;$ S: $(-\infty, -1) \cup (0, 6)$
59. $x^3 - x^2 - x + 1 > 0$
60. $(x+1)(x^2 + 2x - 7) \geq x^2 - 1$ S: $[-3, -1]$
61. $x^4 - 2x^2 \geq 8$ S: $(-\infty, -2] \cup [2, \infty)$
62. $(x^2 + 1)^2 - 7(x^2 + 1) + 10 < 0;$ S: $(-2, -1) \cup (1, 2)$
63. $|x+2| < 1;$ S: $(-3, -1)$
64. $|x-2| \geq 5;$
65. $|2x-1| > 2;$ S: $(-\infty, -\frac{1}{2}) \cup (\frac{3}{2}, \infty)$
66. $|\frac{x}{4} + 1| < 1;$ S: $(-8, 0)$
67. $\left| \frac{2x}{7} - 5 \right| \geq 7;$
68. $|2x-7| > 3;$ S: $(-\infty, 2) \cup (5, \infty)$
69. $|\frac{x}{2} + 7| + 7 \geq 2;$
70. $\left| 2 + \frac{5}{x} \right| > 1;$ S: $(-\infty, -5) \cup (-5/3, 0) \cup (0, \infty)$
71. $|\frac{1}{x} - 3| > 6;$
72. $|x-1| < 2|x-3|;$ S: $(-\infty, \frac{7}{3}) \cup (5, \infty)$
73. $|2x-1| \geq |x+1|;$
74. $2|2x-3| < |x+10|;$ S: $(-\frac{4}{5}, \frac{16}{3})$
75. $|3x-1| < 2|x+6|;$